

Problem 1

A miter saw has an operating speed of 1500 rpm. The blade and motor armature have a combined weight of 3 lbs and a radius of gyration of 1 inch.

- What is the time required for the bearing friction alone ($T = .015$ in lbs) to stop the blade?
- What is the torque a braking system would need to apply to stop the blade in just .25 seconds?



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a)

$$\begin{aligned}
 & \left(\overset{\uparrow}{M} \right) (t) = I \left(\overset{\uparrow}{\omega_f} - \overset{\uparrow}{\omega_i} \right) \\
 & \left(-.015 \text{ in lbs} \right) \left(\frac{1 \text{ ft}}{12 \text{ in}} \right) = \left(\overset{\uparrow}{m} \right) \left(\overset{\uparrow}{k} \right)^2 \left(0 - 157.08 \text{ rad/s} \right) \\
 & \left(\frac{3 \text{ lbs}}{32.2 \frac{\text{ft}}{\text{s}^2}} \right) \left(\frac{1}{12} \text{ ft} \right)^2 \left(-157.08 \text{ rad/s} \right) \\
 & \boxed{t = 81.3 \text{ s} = 1.35 \text{ min}} \quad \text{no brakes}
 \end{aligned}$$

b

$$\begin{aligned}
 & (M) (.25 \text{ s}) = \boxed{I (\omega_f - \omega_i)} \\
 & \quad \quad \quad \text{Same as before} \\
 & \boxed{M = -.406 \text{ ft lbs} = -4.88 \text{ in lbs}} \quad \text{with brakes}
 \end{aligned}$$